Exercise 1 The table below represents the distribution of the number of vehicles per family

| Number of vehicles | Frequency |
| :---: | :---: |
| 0 | 17 |
| 1 | 24 |
| 2 | 28 |
| 3 | 11 |

1. Determine the studied population, the studied characteristic and its nature, as well as its modalities.
2. On a statistical table, represent the cumulative increasing and decreasing frequency $\left(C I n_{i}\right)\left(C D n_{i}\right)$, the relative frequencies.
3. From the table, determine which frequency of families has at most 1 vehicle? At least 2 vehicles?
4. Determine the three quartiles of the statistical series.
5. Calculate the mean and variance of this statistical series.

## Exercise 2

A basket contains 100 oranges. Each orange is weighed, and the number of defects on each orange is counted. Let $X$ denote the mass of each orange in kilograms, and let $Y$ be an integer representing the number of defects per orange. Consequently, the statistical series (see Table below) corresponding to the two variables, which are mass and number of defects, is obtained.

| $\mathbf{X} \mid \mathbf{Y}$ | $[0.1-0.2[$ | $[0.2-0.22[$ | $[0.22-0.24[$ | $[0.24-0.30[$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 1 | 10 | 15 | 4 |
| 1 | 8 | 10 | 12 | 20 |
| 2 | 0 | 2 | 4 | 14 |

- Determine the population, type, and nature of the variables $Y$ and $X$.
- From the statistical table, calculate all marginal frequencies and determine the distribution tables for each of the two variables $Y$ and $X$.
- Calculate the mean and variance of each variable.
- Calculate the covariance $\operatorname{cov}(Y, X)$.
- Calculate the equation of linear regression of $Y$ on $X$.
- calculate the correlation coefficient.

Exercise 3 Suppose a school has two math classes: Advanced and Basic. 30\% of the students are in the Advanced class. In the Advanced class, $90 \%$ of the students pass their final exam. In the Basic class, only $60 \%$ of the students pass the exam.

1. Draw a probability tree for this scenario.
2. Calculate the probability that a randomly selected student passes the exam.
3. Given that a student passed the exam, calculate the probability that they were in the Advanced class.
4. Suppose it is known that a student failed the exam. Calculate the probability that this student was in the Basic class.
